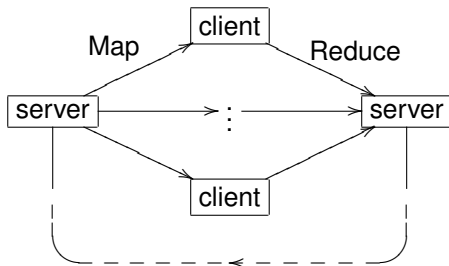


# Dynamic Multirole Session Types

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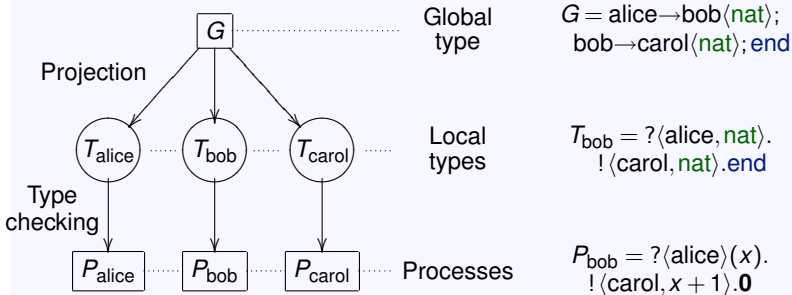
# Multiparty session types (MPST)

- Today's distributed applications involve more and more agents that interact through complex communication patterns.
- Multiparty sessions types can describe these interactions and statically ensure type and communication safety and fidelity to a stipulated protocol.

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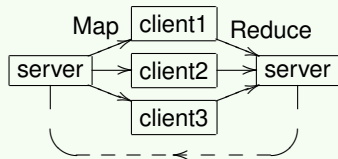
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- Multiparty sessions types can describe these interactions and statically ensure type and communication safety and fidelity to a stipulated protocol.

## Multiparty session types in a nutshell



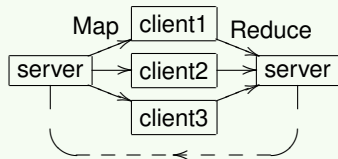
# Multiparty session example

## Map-Reduce in MPST


$$G_{org} = \mu \mathbf{x}. (\text{server} \rightarrow \text{client1} \langle \text{Map} \rangle;$$
$$\text{server} \rightarrow \text{client2} \langle \text{Map} \rangle;$$
$$\text{server} \rightarrow \text{client3} \langle \text{Map} \rangle;$$
$$\text{client1} \rightarrow \text{server} \langle \text{Reduce} \rangle;$$
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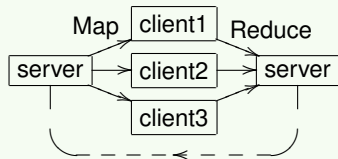

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## Main characteristics and features

- Initial synchronisation
- Fixed number of participants
- Asynchronous semantics
- Communication safety
- Progress

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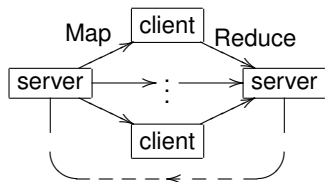
## Main characteristics and features

Initial synchronisation  
Fixed number of participants  
Asynchronous semantics  
Communication safety  
Progress

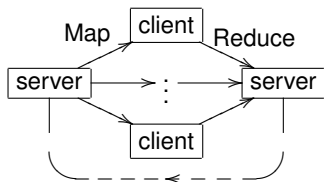
→

Periodic synchronisation  
Variable number of participants  
Explicit parallel composition  
Communication safety  
Progress

# Map-Reduce with dynamic multirole sessions



# Map-Reduce with dynamic multirole sessions



$$G = \mu x. \forall x : \text{client}. \{ \text{server} \rightarrow x \langle \text{Map} \rangle ; \\ x \rightarrow \text{server} \langle \text{Reduce} \rangle \};$$

**x**

## Roles

Two roles (server and client) who each correspond to a communication pattern. Multiple participants can instantiate roles.

## Universal quantification

$\forall x : r. G'$  polls the current participants  $p_1, \dots, p_n$  of role  $r$  and, in parallel processes, binds  $x$  to each in the subsequent interaction, as in

$$\forall x : r. G' \equiv G' \{ p_1 / x \} \mid \dots \mid G' \{ p_n / x \}$$



- I Universal quantification and polling
- II Projection, well-formedness and typing
- III Communication safety and progress
- IV Conclusion

# Global Types

Global types follow standard Multiparty Session Type syntax, with the addition of universal quantification and explicit parallel composition.

$G ::=$		Global types
	$p \rightarrow p' \{l_i \langle \vec{p}_i \rangle \langle U_i \rangle . G_i\}_{i \in I}$	Labelled messages
	$\forall x : r \setminus \vec{p} . G$	Universal quantification
	$G \mid G'$	Parallel composition
	$G ; G'$	Sequential composition
	$\mu \mathbf{x} . G$	Recursion
	$\mathbf{x}$	Recursion variable
	$\varepsilon$	Inaction
	<b>end</b>	End

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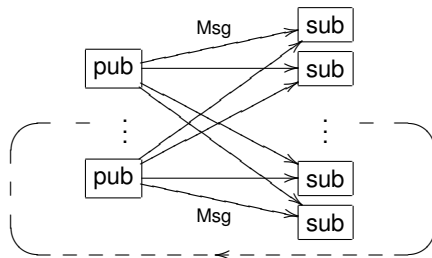
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## Example (Semantical differences)

$$\begin{aligned} G_1 &= \mu \mathbf{x} . \forall x : \text{client} . \{x \rightarrow \text{server} \langle \text{Msg} \rangle . \forall y : \text{client} \setminus x . \{\text{server} \rightarrow y \langle \text{Spread} \rangle\}\}; \mathbf{x} \\ G_2 &= \mu \mathbf{x} . \forall x : \text{client} . \{x \rightarrow \text{server} \langle \text{Msg} \rangle\}; \forall y : \text{client} . \{\text{server} \rightarrow y \langle \text{Digest} \rangle\}; \mathbf{x} \\ G_3 &= \mu \mathbf{x} . \forall x : \text{client} . \{x \rightarrow \text{server} \langle \text{Msg} \rangle ; \text{server} \rightarrow x \langle \text{Answer} \rangle\}; \mathbf{x} \end{aligned}$$

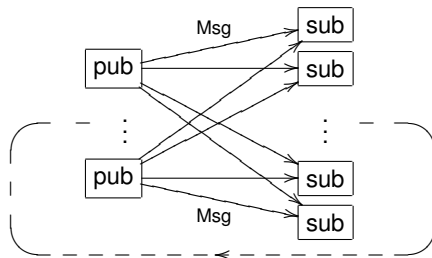
# Publisher-Subscriber example

A set of publishers repeatedly broadcast their messages to a set of subscribers.



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## Global type for Pub-Sub

We write the global type using the universal quantifier for both the pub and the sub roles. The global type is the following:

$$\mu \mathbf{x}. (\forall x : \text{pub}. \forall y : \text{sub}. x \rightarrow y(\text{Msg})); \mathbf{x}$$

# Processes

$u ::= x \mid a \mid b \mid \dots$  Shared channel  
 $p ::= p:r \mid x:r$  Participant with role  
 $\vec{p} ::= p::\vec{p} \mid x::\vec{p} \mid \varepsilon$  Participant list  
 $c ::= s[p] \mid y$  Session channel

$P ::=$  Processes

$u\langle G \rangle$	Session Init	
$u[p](y).P$	Join	$\text{if } e \text{ then } P \text{ else } P$ Conditional
$\text{quit}\langle c \rangle$	Quit	$\mu X.P \mid X \mid \mathbf{0}$ Recursion
$c!\langle p, l(\vec{p}) \rangle(e)$	Send	$(\nu a:G)P$ Restriction
$c?\langle p, \{l_i(\vec{p}_i)(x_i).P_i\}_{i \in I} \rangle$	Receive	$(\nu s)P$ Session restriction
$c\forall(x:r \setminus \vec{p}).\{P\}$	Poll	$s:h$ Message buffer
$P \mid P$	Parallel	$a\langle s \rangle[\mathbb{R}]$ Session registry
$P;P$	Sequential	

## Processes for Pub-Sub

$$P(z:\text{pub}, m) = a[z:\text{pub}](s).\mu X.(s\forall(y:\text{sub}).\{s!\langle y, \text{Msg}\langle m \rangle \rangle\}); X$$
$$P(z:\text{sub}) = a[z:\text{sub}](s).\mu X.(s\forall(x:\text{pub}).\{s?\langle x, \text{Msg}\langle w \rangle \rangle\}); X$$

# Operational semantics

$a\langle s \rangle[R]$  keeps the current list of participants in  $R$ .

$$a\langle G \rangle \rightarrow (v s)(a\langle s \rangle[R] \mid s:\varepsilon) \quad (\forall r_i \in G, R(r_i) = \emptyset) \text{ [INIT]}$$

$$a[p:r](y).P \mid a\langle s \rangle[R \cdot r:P] \rightarrow P\{s[p:r]/y\} \mid a\langle s \rangle[R \cdot r:P \uplus \{p\}] \quad \text{[JOIN]}$$

$$\text{quit}\langle s[p:r] \rangle \mid a\langle s \rangle[R \cdot r:P] \rightarrow a\langle s \rangle[R \cdot r:P \setminus p] \quad \text{[QUIT]}$$

$$s[p:r]!\langle p':r', l\langle \vec{p} \rangle \langle v \rangle \rangle \mid a\langle s \rangle[R] \mid s:h \rightarrow a\langle s \rangle[R] \mid s:h \cdot (p:r, p':r', l\langle \vec{p} \rangle \langle v \rangle) \\ (p \in R(r) \wedge p' \in R(r')) \quad \text{[SEND]}$$

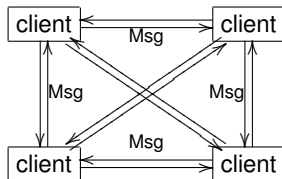
$$s[p:r]?\langle p':r', \{l_j\langle \vec{p}_j \rangle \langle x_j \rangle . P_j\}_{j \in I} \rangle \mid a\langle s \rangle[R] \\ \mid s:(p':r', p:r, l_k\langle \vec{p}_k \rangle \langle v \rangle) \cdot h \rightarrow P_k\{v/x_k\} \mid a\langle s \rangle[R] \mid s:h \\ (p \in R(r) \wedge k \in I) \quad \text{[RECV]}$$

$$s[p:r']\forall(x:r \setminus \vec{p}).\{P\} \mid a\langle s \rangle[R] \rightarrow P\{p_1/x\} \mid \dots \mid P\{p_k/x\} \mid a\langle s \rangle[R] \\ (R(r) \setminus \vec{p} = \{p_1, \dots, p_k\} \wedge p \in R(r')) \quad \text{[POLL]}$$

# Another example: peer-to-peer chat

At every step, each client sends a message to every other client.

$$G = \mu \mathbf{x}. (\forall x : \text{client}. \forall y : \text{client} \setminus x. \{x \rightarrow y \text{Msg} \langle \text{string} \rangle\}); \mathbf{x}$$



## Local Type

$$T_{\text{client}}(z) = \mu \mathbf{x}. (\forall y : \text{client} \setminus z. \{! \langle y, \text{Msg} \langle \text{string} \rangle \rangle\} \mid \forall x : \text{client} \setminus z. \{? \langle x, \text{Msg} \langle \text{string} \rangle \rangle\}); \mathbf{x}$$

How do we go from the global type to the local type?



## Intuition

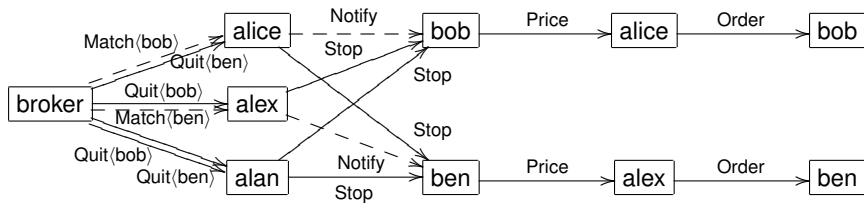
$$\begin{array}{ll}
 (\forall x:r.G) & \uparrow p_j:r \\
 (G\{p_1/x\} \mid \dots \mid G\{p_k/x\}) & \uparrow p_j:r \\
 (G\{p_1/x\} \uparrow p_j:r) \mid \dots \mid (G\{p_k/x\} \uparrow p_j:r) & \\
 (G\{p_i/x\} \uparrow p_j:r) \mid \forall x:r \setminus p_i.(G \uparrow p_j:r) & 
 \end{array}$$

## Main rules

$$\begin{array}{l}
 p \rightarrow p' \{l_i \langle \vec{p}_i \rangle \langle U_i \rangle : G_i\}_{i \in I} \uparrow p = ! \langle p', \{l_i \langle \vec{p}_i \rangle \langle U_i \rangle . G_i \uparrow p\}_{i \in I} \rangle \\
 p' \rightarrow p \{l_i \langle \vec{p}_i \rangle \langle U_i \rangle : G_i\}_{i \in I} \uparrow p = ? \langle p', \{l_i \langle \vec{p}_i \rangle \langle U_i \rangle . G_i \uparrow p\}_{i \in I} \rangle \\
 p \rightarrow p \{l_i \langle \vec{p}_i \rangle \langle U_i \rangle : G_i\}_{i \in I} \uparrow p = ! \langle p, \{l_i \langle \vec{p}_i \rangle \langle U_i \rangle . ? \langle p, l_i \langle \vec{p}_i \rangle \langle U_i \rangle . G_i \uparrow p \}_{i \in I} \rangle \\
 p' \rightarrow p'' \{l_i \langle \vec{p}_i \rangle \langle U_i \rangle . G_i\}_{i \in I} \uparrow p = \bigsqcup_{i \in I} \{G_i \uparrow p\} \\
 (\forall x:r \setminus \vec{p}.G) \uparrow z:r = G\{z/x\} \uparrow z:r \mid \forall x:r \setminus z::\vec{p}.(G \uparrow z:r) \quad (z \notin \vec{p}) \\
 (\forall x:r \setminus \vec{p}.G) \uparrow p = \forall x:r \setminus \vec{p}.(G \uparrow p) \quad (\text{otherwise})
 \end{array}$$

# Auction example, disambiguation of parallel branches

A single broker forms pairs of buyers and sellers.



## Global type for Auction

$$G = \forall x : \text{buyer}. \forall y : \text{seller}. \text{broker} \rightarrow x \{ \text{Match}(y). x \rightarrow y \langle \text{Notify} \rangle. y \rightarrow x \langle \text{Price} \rangle. x \rightarrow y \langle \text{Order} \rangle, \\ \text{Quit}(y). x \rightarrow y \langle \text{Stop} \rangle \}; \text{end}$$

- Syntax correctness

- ×  $G_1 = \mu \mathbf{x} . (\text{server} \rightarrow \text{client} \langle \text{Msg} \rangle ; \mathbf{x} \mid \text{server} \rightarrow \text{broker} \langle \text{Notify} \rangle ; \mathbf{x})$
- ✓  $G_2 = \mu \mathbf{x} . (\text{server} \rightarrow \text{client} \langle \text{Msg} \rangle \mid \text{server} \rightarrow \text{broker} \langle \text{Notify} \rangle) ; \mathbf{x}$
- ✓  $G_3 = \mu \mathbf{x} . \text{server} \rightarrow \text{client} \langle \text{Msg} \rangle ; \mathbf{x} \mid \mu \mathbf{y} . \text{server} \rightarrow \text{broker} \langle \text{Notify} \rangle ; \mathbf{y}$

- Projectability (projection always returns)

- ×  $G_4 = \text{broker} \rightarrow \text{buyer} \{ \text{Notify} . \text{buyer} \rightarrow \text{seller} \langle \text{Msg} \rangle ; \text{seller} \rightarrow \text{buyer} \langle \text{Pay} \rangle , \text{Quit} . \text{buyer} \rightarrow \text{seller} \langle \text{Msg} \rangle \}$
- ✓  $G_5 = \text{broker} \rightarrow \text{buyer} \{ \text{Notify} . \text{buyer} \rightarrow \text{seller} \langle \text{Price} \rangle ; \text{seller} \rightarrow \text{buyer} \langle \text{Pay} \rangle , \text{Quit} . \text{buyer} \rightarrow \text{seller} \langle \text{Stop} \rangle \}$

- Linearity (no possible confusion between parallel branches)

- ×  $G_6 = \forall x : \text{buyer} . \forall y : \text{seller} . \{ \text{broker} \rightarrow x \langle \text{Msg} \rangle . x \rightarrow y \langle \text{Notify} \rangle \}$
- ✓  $G_7 = \forall x : \text{buyer} . \forall y : \text{seller} . \{ \text{broker} \rightarrow x \langle \text{Msg} \langle y \rangle \rangle . x \rightarrow y \langle \text{Notify} \rangle \}$

# Typing system

We show only a selection of rules.

$$\frac{\Gamma \vdash u : \langle G \rangle \quad \Gamma \vdash P \triangleright \Delta, y : G \uparrow p}{\Gamma \vdash u[p](y).P \triangleright \Delta} \text{[JOIN]} \quad \frac{\Gamma \vdash P \triangleright \Delta, c : \text{end}}{\Gamma \vdash \text{quit} \langle c \rangle ; P \triangleright \Delta, c : \text{end}} \text{[LEAVE]}$$

$$\frac{\Gamma, x : r \vdash P \triangleright c : T \quad \Gamma \vdash \vec{p}}{\Gamma \vdash c \forall (x : r \setminus \vec{p}). \{P\} \triangleright c : \forall x : r \setminus \vec{p}. T} \text{[POLLING]}$$

$$\frac{\Gamma \vdash a : \langle G \rangle \quad \{r_i\}_{i \in I} = \text{dom}(R) \quad G \uparrow x_i : r_i = T_i}{\Gamma \vdash_{\emptyset} a \langle s \rangle [R] \triangleright \{s[p_{ji} : r_i] : T_i \setminus \{p_{ji} / x_i\}\}_{i \in I, p_{ji} \notin R(r_i)}} \text{[RGST]} \quad \frac{\Gamma \vdash_{\Sigma_i} P_i \triangleright \Delta_i \quad (i = 1, 2)}{\Gamma \vdash_{\Sigma_1 \uplus \Sigma_2} P_1 \mid P_2 \triangleright \Delta_1 * \Delta_2} \text{[GPAR]}$$

## Theorem (Type safety)

Suppose  $\Gamma \vdash P \triangleright \Delta$ . For any  $P'$  such that  $P \rightarrow^* P'$ ,  $P'$  has no type error.

# Limitations

The semantics and type system are not constrained enough ...

## Leaving a session

The typing rule [LEAVE] only allows a participant to leave when its local type is `end`. It means that if  $G$  is of the form  $\mu \mathbf{x}. G_0; \mathbf{x}; \mathbf{end}$ , no one can leave ...

$$\mu \mathbf{x}. \forall x : \text{client}. \forall y : \text{client} \setminus x. \{x \rightarrow y \text{Msg} \langle \text{string} \rangle\}; \mathbf{x}$$

## Polling consistency for communication safety

$$a[z : \text{client}](s). \mu X. (s \forall (y : \text{client} \setminus z). \{s! \langle y, \text{Msg} \langle m \rangle \rangle\} \\ | s \forall (x : \text{client} \setminus z). \{s? \langle x, \text{Msg} \langle w \rangle \rangle\}); X$$

All local polling operations should give the same list, otherwise messages are unexpected or absent.

# Multiparty locking

We need to temporarily *block* late participants from joining in the middle of a session execution in order to prevent any interference with polling: we automatically introduce a locking mechanism  $\text{lock}\{G\}$ .

$$\mu x. \text{lock}\{\forall x:\text{client}. \forall y:\text{client} \setminus x. \{x \rightarrow y \text{Msg}\langle \text{string} \rangle\}\}; x$$

## Syntax and semantics

$$P ::= \dots \mid c \text{ lock} \mid c \text{ unlock} \mid a^\circ[R, \Lambda] \mid a^\bullet[R, \Lambda]$$

$$\Lambda ::= \emptyset \mid \Lambda \cup \{p:r\}$$

$$s[p:r] \text{ lock} \mid a^\circ\langle s \rangle[R] \rightarrow a^\circ\langle s \rangle[R, \{p:r\}] \quad [\text{LOCK}]$$

$$s[p:r] \text{ lock} \mid a^\circ\langle s \rangle[R, \Lambda] \rightarrow \begin{cases} a^\circ\langle s \rangle[R, \Lambda \uplus \{p:r\}] & (R \not\approx \Lambda \uplus \{p:r\}) \quad [\text{UP}] \\ a^\bullet\langle s \rangle[R, \Lambda \uplus \{p:r\}] & (R \approx \Lambda \uplus \{p:r\}) \quad [\text{TOP}] \end{cases}$$

$$s[p:r] \text{ unlock} \mid a^\bullet\langle s \rangle[R, \Lambda \uplus \{p:r\}] \rightarrow \begin{cases} a^\bullet\langle s \rangle[R, \Lambda] & (\Lambda \neq \emptyset) \quad [\text{DOWN}] \\ a^\circ\langle s \rangle[R] & (\Lambda = \emptyset) \quad [\text{UNLOCK}] \end{cases}$$

$$s[p:r]! \langle p':r', l \langle \vec{p} \rangle \langle v \rangle \rangle \mid a^\bullet\langle s \rangle[R, \Lambda] \mid s:h \rightarrow a^\bullet\langle s \rangle[R, \Lambda] \mid s:h \cdot (p:r, p':r', l \langle \vec{p} \rangle \langle v \rangle)$$

$$\dots \quad [\text{SEND}]$$

## Typing locks

$$G ::= \dots \mid \text{lock}\{G\} \quad T ::= \dots \mid \text{lock} \mid \text{unlock}$$

Well-locked global types are of the form  $\text{lock}\{G_0\}; \text{end}$ .

Persistently well-locked global types are of the form  $\mu x. \text{lock}\{G_0\}; x; \text{end}$

$$\text{lock}\{G\} \uparrow z:r = \text{lock}; (G \uparrow z:r); \text{unlock}$$
$$\frac{\Gamma \vdash \text{Env}}{\Gamma \vdash c \text{ lock} \triangleright c:\text{lock}} \quad \frac{\Gamma \vdash \text{Env}}{\Gamma \vdash c \text{ unlock} \triangleright c:\text{unlock}} \quad \frac{\Gamma \vdash P \triangleright \Delta, c:\text{end} \quad \Gamma \vdash u:\langle G \rangle}{\Gamma \vdash \text{quit}\langle c \rangle; P \triangleright \Delta, c:G \uparrow p}$$

## Single iteration chat client

$$P_{\text{client}}(p) = a[p:\text{client}](s). (s \text{ lock}; s \forall (y:\text{client} \setminus z). \{s! \langle y, \text{Msg}\langle m \rangle\} \} \mid \\ s \forall (x:\text{client} \setminus z). \{s? \langle x, \text{Msg}\langle w \rangle\} \}); s \text{ unlock}; \\ \text{quit}\langle s \rangle$$

## Theorem (Communication Safety)

*Every sent message is expected by a receiver. Every receiver will receive a message.*

## Theorem (Progress)

*Well-locked and well-typed processes do not reach a deadlock state.*

## Theorem (Join progress)

*Persistently well-locked and well-typed processes can progress and integrate new joiners.*



- An extension to OCaml
- The compiler generates from the global type a tailored runtime
- The runtime deals with transport (UDP, TCP, AMQP) and registry
- A continuation-based programming interface

## Dynamic multirole session types

- A conservative extension of multiparty session types
- A new universal quantification to ease programming and typing
- Strong safety and progress guarantees at the price of synchronisation

## Ongoing work

- Automatically distribute the registry
- Give a structure (topology) to role participants
- Getting rid of some aspects of the synchronisation

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Thanks