

# Dependent Event Types

Zhaohui Luo<sup>1</sup>(✉) and Sergei Soloviev<sup>2</sup>

<sup>1</sup> Royal Holloway, University of London, Egham, Surrey, UK

`zhaohui.luo@hotmail.co.uk`

<sup>2</sup> IRIT, Toulouse, France

`Sergei.Soloviev@irit.fr`

**Abstract.** This paper studies how dependent types can be employed for a refined treatment of event types, offering a nice improvement to Davidson’s event semantics. We consider dependent event types indexed by thematic roles and illustrate how, in the presence of refined event types, subtyping plays an essential role in semantic interpretations. We consider two extensions with dependent event types: first, the extension of Church’s simple type theory as employed in Montague semantics that is familiar with many linguistic semanticists and, secondly, the extension of a modern type theory as employed in MTT-semantics. The former uses subsumptive subtyping, while the latter uses coercive subtyping, to capture the subtyping relationships between dependent event types. Both of these extensions have nice meta-theoretic properties such as normalisation and logical consistency; in particular, we shall show that the former can be faithfully embedded into the latter and hence has expected meta-theoretic properties. As an example of applications, it is shown that dependent event types give a natural solution to the incompatibility problem (sometimes called the event quantification problem) in combining event semantics with the traditional compositional semantics, both in the Montagovian setting with the simple type theory and in the setting of MTT-semantics.

## 1 Introduction

The event semantics, whose study was initiated by Davidson [6] and further studied in its neo-Davidsonian turn (see [17] among others), has several notable advantages including Davidson’s original motive to provide a satisfactory semantics for adverbial modifications. Dependent types, as those found in Modern Type Theories such as Martin-Löf’s type theory [15] and UTT [11], provide a useful tool in formalising event types and a nice treatment of the event semantics.

In this paper, we shall study event types that may depend on thematic roles such as agents and patients of the events. For example, we can consider the type

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`zhaohui.luo@hotmail.co.uk`

$Evt_{AP}(a, p)$  of events whose agent and patient are  $a$  and  $p$ , respectively. We shall investigate subtyping relations between event types which include dependent types such as  $Evt_{AP}(a, p)$  and the non-dependent type  $Event$  of all events (the latter is found in the traditional setting). For example, it may be natural to have  $Evt_{AP}(a, p) \leq Evt_A(a)$ , that is, the type of events with agent  $a$  and patient  $p$  is a subtype of that with agent  $a$ . With such subtyping relations in place, the semantics of verb phrases can now take the usual non-dependent types, as in the traditional setting, although dependent event types are considered.

It is shown that such dependent event types give a natural solution to the incompatibility problem in combining event semantics with the traditional Montague semantics [2, 20] (sometimes called the event quantification problem [7]). When introducing events into formal semantics, one faces a problem, which is long-standing and has seemed intractable: it comes from the issue of scopes for two kinds of quantifiers – the existential quantifier over an event variable and the other quantifiers such as one that arises from a quantificational noun phrase (see Sect. 5 for examples). It is in general expected that the correct semantics is obtained when the event quantifier takes the lower scope, but the problem is that, even when the event quantifier takes a wider scope, which would give an incorrect semantics, the resulting semantic formula is still well-formed formally. This has led to many proposals such as that considered by Champollion [2] or the related Scope Domain Principle proposed by Landman [9], but all of them are rather ad hoc. Dependent event types will solve this problem: they give a solution where the correct semantics are accepted while the incorrect ones are excluded by typing because they would be ill-typed and hence formally illegal.

Dependent event types (DETs) were first considered in an example in [1] to study linguistic coercions in formal semantics, where types of events are indexed by their agents:  $Evt(h)$  is the type of events conducted by  $h$ : *Human*. In this paper, we shall study event types dependent on thematic roles in event semantics both in the traditional Montague semantics [16] and in formal semantics in modern type theories (MTT-semantics, for short) [4, 13, 18]. For the former, we extend Church’s simple type theory [5], as employed in Montague semantics that is familiar with many linguistic semanticists, by means of dependent event types, resulting in the system  $C_e$ , where the subtyping relationships between DETs are captured by subsumptive subtyping. For the latter, we extend an MTT (in particular, the type theory UTT [11]) with DETs whose subtyping relationships are reflected by coercive subtyping [12, 14], resulting in the type system UTT[E]. Both of these extensions have nice meta-theoretic properties such as normalisation and logical consistency; in particular, we shall show that  $C_e$  can be faithfully embedded into UTT[E] and hence has desirable properties.

The rest of the paper is organised as follows. In Sect. 2, we shall describe the basics of DETs, introducing notations and examples. Subtyping between event types is described in Sect. 3, where we show, for example, how VPs can take the traditional non-dependent type, while we consider DETs. The formal systems  $C_e$  and UTT[E] and the embedding of  $C_e$  in UTT[E] are studied in Sect. 4. Section 5 considers the solution of the event quantification problem by means of DETs:

Sect. 5.1 shows examples in the Montagovian setting and Sect. 5.2 considers it in MTT-semantics. The concluding section briefly discusses the future work.

## 2 Dependent Event Types

In the Davidsonian event semantics in the traditional Montagovian setting [6, 17], there is only one type *Event* of all events. For example, the sentence (1) is interpreted as (2):

- (1) John kissed Mary passionately.  
 (2)  $\exists e: \textit{Event}. \textit{kiss}(e) \ \& \ \textit{agent}(e, j) \ \& \ \textit{patient}(e, m) \ \& \ \textit{passionate}(e)$

where in (2), *Event* is the type of all events, *kiss*, *passionate*: *Event*  $\rightarrow$  **t** are predicates over events, and *agent*, *patient*: *Event*  $\rightarrow$  **e**  $\rightarrow$  **t** are relations between events and entities.<sup>1</sup> Please note that, in the above neo-Davidson's semantics (2), adverbial modifications and thematic role relations are all propositional conjuncts in parallel with the verb description, an advantageous point as compared with an interpretation without events.

We propose to consider refined types of events. Rather than a single type *Event* of events, we introduce types of events that are dependent on some parameters. For instance, an event type can be dependent on agents and patients. Let *Agent* and *Patient* be the types of agents and patients, respectively. Then, for  $a: \textit{Agent}$  and  $p: \textit{Patient}$ , the dependent type

$$\textit{Evt}_{AP}(a, p)$$

is the type of events whose agents are  $a$  and whose patients are  $p$ . With such dependent event types, the above sentence (1) can now be interpreted as:<sup>2</sup>

- (3)  $\exists e: \textit{Evt}_{AP}(j, m). \textit{kiss}(e) \ \& \ \textit{passionate}(e)$

Note that, besides other things we are going to explain below, we do not need to consider the relations *agent* and *patient* as found in (2) because they can now be 'recovered' from typing. For example, for  $a: \textit{Agent}$  and  $p: \textit{Patient}$ , we

<sup>1</sup> In logical formulas or lambda-expressions, people often omit the type labels of events and entities: for example, (2) would just be written as  $\exists e. \textit{kiss}(e) \ \& \ \textit{agent}(e, j) \ \& \ \textit{patient}(e, m) \ \& \ \textit{passionate}(e)$ , since traditionally there are only one type of events and one type of entities; we shall put in the type labels explicitly. Another note on notations is: **e** and **t** in boldface stand for the type of entities and the type of truth values, respectively, as in MG, while  $e$  and  $t$  not in boldface stand for different things (for example,  $e$  would usually be used as a variable of an event type).

<sup>2</sup> Please note here that, for  $\textit{kiss}(e)$  and  $\textit{passionate}(e)$  to be well-typed, the type of event  $e$  must be the same as the domain of *kiss* and *passionate* – see the next section about subtyping, which allows them to be well-typed.

can define functions  $\text{AGENT}_{AP}[a, p]$  and  $\text{PATIENT}_{AP}[a, p]$  such that, for any event  $e$ :  $\text{Evt}_{AP}(a, p)$ ,  $\text{AGENT}_{AP}[a, p](e) = a$  and  $\text{PATIENT}_{AP}[a, p](e) = p$ .<sup>3</sup>

The parameters of dependent event types are usually names of thematic roles such as agents and patients. Formally, the dependent event types are parameterised by objects of types  $A_1, \dots, A_n$ . Event types with  $n$  parameters are called  $n$ -ary event types. In this paper, we shall only consider  $n$ -ary event types with  $n = 0, 1, 2$ :

- When  $n = 0$ , the event type, usually written as *Event*, has no parameters. *Event* corresponds to the type of all events in the traditional setting.
- When  $n = 1$ , we only consider  $\text{Evt}_A(a)$  and  $\text{Evt}_P(p)$ , where  $a$ : *Agent* and  $p$ : *Patient*; i.e., these are event types dependent on agents  $a$  and those dependent on patients  $p$ . For example, if John is an agent with interpretation  $j$ ,  $\text{Evt}_A(j)$  is the type of events whose agents are John.
- When  $n = 2$ , we only consider  $\text{Evt}_{AP}(a, p)$  for  $a$ : *Agent* and  $p$ : *Patient*, i.e., the event type dependent on agent  $a$  and patients  $p$ . For example, if agent John and patient Mary,  $\text{Evt}_{AP}(j, m)$  is the type of events whose agents and patients are John and Mary, respectively (cf., the example (3) above).

Introducing dependent event types has several advantages. In this paper, we shall detail one of them, that is, it gives a natural solution to the event quantification problem – see Sect. 5. Before doing that, we shall first consider in Sect. 3 the subtyping relationship between event types which, among other things, simplifies the semantic interpretations of VPs in the semantics with dependent event types, and then in Sect. 4 the formal systems that underlie the proposed semantic treatments and their meta-theoretic properties.

### 3 Subtyping Between Event Types

Event types have natural subtyping relationships between them. For example, an event whose agent is  $a$  and patient is  $p$  is an event with agent  $a$ . In other words, for  $a$ : *Agent* and  $p$ : *Patient*, the type  $\text{Evt}_{AP}(a, p)$  is a subtype of  $\text{Evt}_A(a)$ . If we only consider the event types *Event*,  $\text{Evt}_A(a)$ ,  $\text{Evt}_P(p)$  and  $\text{Evt}_{AP}(a, p)$  (cf., the last section), they have the following subtyping relationships:

$$\text{Evt}_{AP}(a, p) \leq \text{Evt}_A(a) \leq \text{Event}$$

$$\text{Evt}_{AP}(a, p) \leq \text{Evt}_P(p) \leq \text{Event}$$

which can be depicted as Fig. 1.

Formally, the subtyping relationship obeys the following rule (called subsumption rule):

$$(*) \quad \frac{a: A \quad A \leq B}{a: B}$$

<sup>3</sup> Formally, we have  $\text{AGENT}_{AP}[a, p] = \lambda e : \text{Evt}_{AP}(a, p).a$ , of type  $\text{Evt}_{AP}(a, p) \rightarrow \text{Agent}$ . Usually we simply write, for example,  $\text{AGENT}_{AP}(e)$  for  $\text{AGENT}_{AP}[a, p](e)$ .



*Remark 1.* The subtyping relations also facilitate a natural relationship between the functions such as  $\text{AGENT}_{AP}$  and  $\text{AGENT}_A$  (see Sect. 2 and Footnote 3). For example, because of the subtyping relations as depicted in Fig. 1, for  $e: \text{Evt}_{AP}(a, p) \leq \text{Evt}_A(a)$ , we have, by definition:  $\text{AGENT}_{AP}[a, p](e) = \text{AGENT}_A[a](e) = a$ .

## 4 The Underlying Systems $C_e$ and $\text{UTT}[\mathbf{E}]$

In this section, we describe the formal systems  $C_e$  and  $\text{UTT}[\mathbf{E}]$ :  $C_e$  extends the simple type theory [5] and  $\text{UTT}[\mathbf{E}]$  extends the modern type theory  $\text{UTT}$  [11], both with dependent event types and their subtyping relationships as informally described in Sects. 2 and 3.<sup>5</sup>  $C_e$  is the underlying type theory when we consider formal semantics in the traditional Montagovian setting (as familiar by most of the linguistic semanticists) and  $\text{UTT}[\mathbf{E}]$  when we consider formal semantics in a modern type theory (see, for example, [4, 13]). We also outline the construction of an embedding of  $C_e$  into  $\text{UTT}[\mathbf{E}]$  that shows that, like  $\text{UTT}[\mathbf{E}]$ ,  $C_e$  has nice meta-theoretic properties such as normalisation and logical consistency.<sup>6</sup>

### 4.1 The Types System $C_e$

We shall first explain what a context is and what a judgement is in the system  $C_e$ , and then describe the rules of  $C_e$ .

*Contexts.* A context is a sequence of entries either of the form  $x: A$  or of the form  $P \text{ true}$ . Informally, the former assumes that the variable  $x$  be of type  $A$  and the latter that the proposition  $P$  be true. Only valid contexts are legal and context validity is governed by the following rules:

$$\frac{}{\langle \rangle \text{ valid}} \quad \frac{\Gamma \vdash A \text{ type} \quad x \notin FV(\Gamma)}{\Gamma, x: A \text{ valid}} \quad \frac{\Gamma \vdash P: \mathbf{t}}{\Gamma, P \text{ true valid}}$$

where  $\langle \rangle$  is the empty sequence and  $FV(\Gamma)$  is the set of free variables in  $\Gamma$  defined as: (1)  $FV(\langle \rangle) = \emptyset$ ; (2)  $FV(\Gamma, x: A) = FV(\Gamma) \cup \{x\}$ ; (3)  $FV(\Gamma, P \text{ true}) = FV(\Gamma)$ .

*Judgements.* Judgements are sentences in  $C_e$ , whose correctness are governed by the inference rules below. In  $C_e$ , there are five forms of judgements:

- $\Gamma \text{ valid}$ , which means that  $\Gamma$  is a valid context (the rules of deriving context validity are given above).

<sup>5</sup> A notational remark: in  $C_e$ ,  $C$  stands for ‘Church’ and  $e$  for ‘event’. The notation  $\text{UTT}[\mathbf{E}]$  comes from the work of coercive subtyping (see, for example, [14]) where  $\text{T}[\mathbf{C}]$  denotes type theory  $\text{T}$  extended by coercive subtyping whose basic subtyping are given as the set  $\mathbf{C}$  of subtyping judgements.

<sup>6</sup> This section is rather formal and, for a reader less interested in formal matters, its details might be safely skipped if one wishes so.

$\frac{\Gamma \text{ valid}}{\Gamma \vdash \mathbf{e} \text{ type}}$	$\frac{\Gamma \text{ valid}}{\Gamma \vdash \mathbf{t} \text{ type}}$	$\frac{\Gamma, x:A, \Gamma' \text{ valid}}{\Gamma, x:A, \Gamma' \vdash x : A}$	$\frac{\Gamma, P \text{ true}, \Gamma' \text{ valid}}{\Gamma, P \text{ true}, \Gamma' \vdash P \text{ true}}$
$\frac{\Gamma \vdash A \text{ type} \quad \Gamma \vdash B \text{ type}}{\Gamma \vdash A \rightarrow B \text{ type}}$	$\frac{\Gamma, x:A \vdash b : B \quad x \notin FV(B)}{\Gamma \vdash \lambda x:A.b : A \rightarrow B}$	$\frac{\Gamma \vdash f : A \rightarrow B \quad \Gamma \vdash a : A}{\Gamma \vdash f(a) : B}$	
$\frac{\Gamma \vdash P : \mathbf{t} \quad \Gamma \vdash Q : \mathbf{t}}{\Gamma \vdash P \supset Q : \mathbf{t}}$	$\frac{\Gamma, P \text{ true} \vdash Q \text{ true}}{\Gamma \vdash P \supset Q \text{ true}}$	$\frac{\Gamma \vdash P \supset Q \text{ true} \quad \Gamma \vdash P \text{ true}}{\Gamma \vdash Q \text{ true}}$	
$\frac{\Gamma \vdash A \text{ type} \quad \Gamma, x:A \vdash P : \mathbf{t}}{\Gamma \vdash \forall(A, x.P) : \mathbf{t}}$	$\frac{\Gamma, x:A \vdash P \text{ true}}{\Gamma \vdash \forall(A, x.P) \text{ true}}$	$\frac{\Gamma \vdash \forall(A, x.P[x]) \text{ true} \quad \Gamma \vdash a : A}{\Gamma \vdash P[a] \text{ true}}$	

**Fig. 2.** Rules for Church's STT.

- $\Gamma \vdash A \text{ type}$ , which means that  $A$  is a type under context  $\Gamma$ .
- $\Gamma \vdash a : A$ , which means that  $a$  is an object of type  $A$  under context  $\Gamma$ .
- $\Gamma \vdash P \text{ true}$ , which means that  $P$  is a true proposition under context  $\Gamma$ .
- $\Gamma \vdash A \leq B$ , which means that  $A$  is a subtype of  $B$  under context  $\Gamma$ .

*Inference Rules.* The inference rules for  $C_e$  consist of:

1. Rules for context validity (the three rules above);
2. Figure 2: the rules for Church's simple type theory including those for (1) the basic types  $\mathbf{e}$  and  $\mathbf{t}$  of entities and truth values, (2) function types with  $\beta$ -conversion  $((\lambda x : A.b[x])(a) \simeq b[a])$ , and (3) logical formulas<sup>7</sup>; and
3. Figure 3: the rules for dependent event types including those for (1) dependent event types and (2) their subtyping relations, and (3) general subtyping rules including subsumption.

Some explanations of the rules are in order:

- In the  $\lambda$ -rule in Fig. 2, we have added a side condition  $x \notin FV(B)$ , i.e.,  $x$  does not occur free in  $B$ . This is necessary because we have dependent event types like  $Evt_A(a)$ : for example, we need to forbid to derive  $\Gamma \vdash (\lambda x : Agent.\lambda e : Evt_A(x).e) : Agent \rightarrow Evt_A(x) \rightarrow Evt_A(x)$  from  $\Gamma, x : Agent \vdash (\lambda e : Evt_A(x).e) : Evt_A(x) \rightarrow Evt_A(x)$ , where in the former judgement,  $x$  in  $Agent \rightarrow Evt_A(x) \rightarrow Evt_A(x)$  would be a free variable that has not been declared in  $\Gamma$ . Note that, in Church's formulation [5], the side condition is not needed because, there, there are no dependent types (and  $x$  does not occur free in  $B$  for sure).
- In the rules in Fig. 3, since all of the judgements have the same contexts, we have omitted the contexts. For example, the first rule in its third row should have been, if written in full:

$$\frac{\Gamma \vdash a : Agent \quad \Gamma \vdash p : Patient}{\Gamma \vdash Evt_{AP}(a, p) \leq Evt_A(a)}$$

<sup>7</sup> We only consider the intuitionistic  $\supset$  and  $\forall$  here, omitting other operators including, in particular, those about, e.g. negation/classical logic in [5]. Also, we shall not assume extensionality.

	<i>Agent type</i>	<i>Patient type</i>	
<i>Event type</i>	$a : \text{Agent}$	$p : \text{Patient}$	$a : \text{Agent} \quad p : \text{Patient}$
	$\text{Evt}_A(a)$ type	$\text{Evt}_P(p)$ type	$\text{Evt}_{AP}(a, p)$ type
	$a : \text{Agent} \quad p : \text{Patient}$	$a : \text{Agent} \quad p : \text{Patient}$	
	$\text{Evt}_{AP}(a, p) \leq \text{Evt}_A(a)$	$\text{Evt}_{AP}(a, p) \leq \text{Evt}_P(p)$	
	$a : \text{Agent}$	$p : \text{Patient}$	
	$\text{Evt}_A(a) \leq \text{Event}$	$\text{Evt}_P(p) \leq \text{Event}$	
<i>A type</i>	$A \leq B \quad B \leq C$	$A' \leq A \quad B \leq B'$	
$A \leq A$	$A \leq C$	$A \rightarrow B \leq A' \rightarrow B'$	
	$A \simeq B$	$a : A \quad A \leq B$	
	$A \leq B$	$a : B$	

**Fig. 3.** Rules for dependent event types.

## 4.2 The Type System $\text{UTT}[\mathbf{E}]$

The type theory  $\text{UTT}$  (Chap. 9 of [11]) is a dependent type theory with inductive types, type universes and higher-order logic.  $\text{UTT}$  is a typical Modern Type Theory (MTT) as employed in MTT-semantics [4, 13] (actually, it is the MTT the first author and colleagues have employed in developing MTT-semantics). Its meta-theory was studied in the Ph.D. thesis by Goguen [8]. Coercive subtyping [12, 14] has been developed by the authors and colleagues for modern type theories such as Martin-Löf's type theory and  $\text{UTT}$ .

Besides the type constructors in  $\text{UTT}$  as described in [11],  $\text{UTT}[\mathbf{E}]$  has the following constant types and constant type families for dependent event types:

- *Entity*: *Type*
- *Agent*, *Patient*: *Type*.
- *Event*: *Type*,
- $\text{Evt}_A$ : (*Agent*)*Type*,
- $\text{Evt}_P$ : (*Patient*)*Type*, and
- $\text{Evt}_{AP}$ : (*Agent*)(*Patient*)*Type*.

The coercive subtyping relations in  $\text{UTT}[\mathbf{E}]$  are given by subtyping judgements in  $\mathbf{E}$ : they specify the subtyping relationships between dependent event types by means of the following parameterised constant coercions  $c_i$  ( $i = 1, \dots, 4$ ) in  $\mathbf{E}$ , where  $a$ : *Agent* and  $p$ : *Patient*:

$$\text{Evt}_{AP}(a, p) \leq_{c_1[a, p]} \text{Evt}_A(a), \quad \text{Evt}_{AP}(a, p) \leq_{c_2[a, p]} \text{Evt}_P(p),$$

$$\text{Evt}_A(a) \leq_{c_3[a]} \text{Event}, \quad \text{Evt}_P(p) \leq_{c_4[p]} \text{Event},$$

The coercions also satisfy the coherence condition  $c_3[a] \circ c_1[a, p] = c_4[p] \circ c_2[a, p]$ .

Based on the study in [14,21], it is straightforward to show that  $\text{UTT}[\mathbf{E}]$  is a well-behaved extension of  $\text{UTT}$  and hence preserves its nice meta-theoretic properties, including Church-Rosser, subject reduction, strong normalisation, and logical consistency.

*Remark 2.* As mentioned above,  $\text{UTT}[\mathbf{E}]$  underlies the development of MTT-semantics by the first author and colleagues [4,13]. In the recent trend of using rich type theories in formal semantics (see, for example, some of the papers in [3]), the development of MTT-semantics provides a full-blown alternative to the traditional Montague semantics with many advantages and has its further potentials to be developed in the future. It is worth remarking that  $\text{UTT}[\mathbf{E}]$  underlies the event semantics in dependent type theories (or MTT-semantics with events) which contain, in particular, dependent event types.

### 4.3 Embedding of $\mathcal{C}_e$ into $\text{UTT}[\mathbf{E}]$

In this subsection, we show that  $\mathcal{C}_e$  can be faithfully embedded into  $\text{UTT}[\mathbf{E}]$  and hence has nice meta-theoretic properties. The embedding of  $\mathcal{C}_e$  into  $\text{UTT}[\mathbf{E}]$  is defined as follows and it is faithful as the theorem below shows.

**Definition 1 (embedding).** *The embedding  $\llbracket \_ \rrbracket$  from  $\mathcal{C}_e$  to  $\text{UTT}[\mathbf{E}]$  is inductively defined as follows:<sup>8</sup>*

1. *Constant types and dependent event types:*

- $\llbracket \mathbf{e} \rrbracket_\Gamma = \text{Entity}$ .
- $\llbracket \mathbf{t} \rrbracket_\Gamma = \text{Prop}$ .

*For the other constant types and dependent event types, they are mapped to the ‘same’ types in  $\text{UTT}[\mathbf{E}]$ , since we have overloaded their names. For example,*

- $\llbracket \text{Agent} \rrbracket = \text{Agent}$
- $\llbracket \text{Evt}_A(a) \rrbracket = \text{Evt}_A(\llbracket a \rrbracket)$

2. *Non-constant terms:*

- $\llbracket x \rrbracket_\Gamma = x$
- $\llbracket A \rightarrow B \rrbracket_\Gamma = \llbracket A \rrbracket_\Gamma \rightarrow \llbracket B \rrbracket_\Gamma$
- $\llbracket \lambda x : A. b \rrbracket_\Gamma = \lambda(\llbracket A \rrbracket_\Gamma, T, [x : \llbracket A \rrbracket_\Gamma] \llbracket b \rrbracket_{\Gamma, x:A}),$  if  $\llbracket \Gamma, x : A \rrbracket \vdash \llbracket b \rrbracket_{\Gamma, x:A} : T$
- $\llbracket f(a) \rrbracket_\Gamma = \text{app}(S, T, \llbracket f \rrbracket_\Gamma, \llbracket a \rrbracket_\Gamma),$  if  $\llbracket \Gamma \rrbracket \vdash \llbracket f \rrbracket_\Gamma : S \rightarrow T$  and  $\llbracket \Gamma \rrbracket \vdash \llbracket a \rrbracket_\Gamma : S_0,$  where  $\llbracket \Gamma \rrbracket \vdash S_0 \leq S$
- $\llbracket P \supset Q \rrbracket_\Gamma = \llbracket P \rrbracket_\Gamma \supset \llbracket Q \rrbracket_\Gamma$
- $\llbracket \forall(A, x.P) \rrbracket_\Gamma = \forall(\llbracket A \rrbracket_\Gamma, [x : \llbracket A \rrbracket_\Gamma]. \llbracket P \rrbracket_{\Gamma, x:A})$

3. *Contexts:*

- $\llbracket \langle \rangle \rrbracket = \langle \rangle$  (the empty context in  $\text{UTT}[\mathbf{E}]$ )
- $\llbracket \Gamma, x : A \rrbracket = \llbracket \Gamma \rrbracket, x : \llbracket A \rrbracket_\Gamma$

<sup>8</sup> Formally, this is a partial function – it is only defined when certain conditions hold. The embedding theorem shows that the embedding is total for well-typed terms. Also, a notional note: we shall use  $S$  and  $T$  to stand for types in  $\text{UTT}[\mathbf{E}]$  where function types are special cases of  $\Pi$ -types: for any types  $S$  and  $T$ ,  $S \rightarrow T = \Pi(S, [- : S]T)$ .

–  $\llbracket \Gamma, P \text{ true} \rrbracket = \llbracket \Gamma \rrbracket, x: \mathbf{Prf}(\llbracket P \rrbracket_\Gamma)$ , where  $x$  does not occur free in  $\llbracket \Gamma \rrbracket$ .

The following theorem shows that the embedding is well-defined and faithful (in the sense of the theorem) and hence  $\mathcal{C}_e$  has nice meta-theoretic properties (the corollary). Its proof is based on the embedding of Church’s simple type theory into the calculus of constructions [10]. We omit the discussion of technical details, for otherwise we would have to detail the syntax and rules of UTT and coercive subtyping [11,14], except remarking that a key reason that the proof goes through is because the coercions to model subtyping for dependent event types are constants and coherent (see Sect.4.2) and hence model subsumptive subtyping in  $\mathcal{C}_e$  faithfully.

**Theorem 2 (faithfulness).** *The embedding in Definition 1 is defined for every well-typed term in  $\mathcal{C}_e$  and, furthermore, we have:*

1. If  $\Gamma$  valid in  $\mathcal{C}_e$ , then  $\llbracket \Gamma \rrbracket$  valid in  $UTT[E]$ .
2. If  $\Gamma \vdash A$  type in  $\mathcal{C}_e$ , then  $\llbracket \Gamma \rrbracket \vdash \llbracket A \rrbracket$ : Type in  $UTT[E]$ .
3. If  $\Gamma \vdash a: A$  in  $\mathcal{C}_e$ , then in  $UTT[E]$ ,  $\llbracket \Gamma \rrbracket \vdash \llbracket a \rrbracket: T$  for some  $T$  such that  $\llbracket \Gamma \rrbracket \vdash T \leq_d \llbracket A \rrbracket$  for some  $d$ .
4. If  $\Gamma \vdash P$  true in  $\mathcal{C}_e$ , then  $\llbracket \Gamma \rrbracket \vdash p: \mathbf{Prf}(\llbracket P \rrbracket)$  for some  $p$  in  $UTT[E]$ .
5. If  $\Gamma \vdash A \leq B$  in  $\mathcal{C}_e$ , then  $\llbracket \Gamma \rrbracket \vdash \llbracket A \rrbracket \leq_c \llbracket B \rrbracket$  for some unique  $c$  in  $UTT[E]$ .

**Corollary 3.**  *$\mathcal{C}_e$  inherits nice meta-theoretic properties from  $UTT[E]$ , including strong normalisation and logical consistency.*

*Remark 3.* Instead of the embedding method we have described here, one may consider a more direct approach to metatheory of  $\mathcal{C}_e$  by directly showing that it has nice properties such as Church-Rosser and strong normalisation (as suggested by an anonymous reviewer). However, we think the above is simpler, which is of course a subjective view, and also demonstrates a generic approach to such meta-theoretic studies.

## 5 Event Quantification Problem

It is known that, when considering (neo-)Davidsonian event semantics where existential quantifiers for event variables are introduced, there is a problem in dealing with the scopes of the quantifiers when other quantificational phrases are involved. It has been argued that there is some incompatibility between event semantics and the traditional compositional semantics [2,20]. De Groote and Winter [7] have called this as the *event quantification problem* (EQP for short).

Consider the following sentence (8) which, under the traditional event semantics with  $bark: Event \rightarrow \mathbf{t}$ , could have two possible interpretations (9) and (10), where (10) is incorrect.

- (8) No dog barks.
- (9)  $\neg \exists x: \mathbf{e}. dog(x) \ \& \ \exists e: Event. bark(e) \ \& \ agent(e, x)$
- (10)  $(\#) \exists e: Event. \neg \exists x: \mathbf{e}. dog(x) \ \& \ bark(e) \ \& \ agent(e, x)$

Formally, the incorrect interpretation is acceptable just as the correct one: (10) is a legal formula. In order to avoid such incorrect interpretations as (10), people have made several proposals (see, for example, [2, 20]) which involve, for instance, consideration of quantification not over events but over sets of events [2], or some informal (and somewhat *ad hoc*) principles whose adherence would disallow the incorrect interpretations (see, for example, the related Scope Domain Principle proposed by Landman [9]).

We shall study this with dependent event types as informally studied in Sects. 2 and 3, both in the Montagovian setting (i.e., in  $C_e$  as described in Sect. 4.1) and in the MTT-semantic (i.e., in  $UTT[E]$  as described in Sect. 4.2). It is shown that, with dependent event types, the incorrect semantics are blocked as illegal since they are ill-typed.

### 5.1 EQP in Montague Semantics with Dependent Event Types

In the Montagovian setting with dependent event types (formally,  $C_e$  in Sect. 4.1), this problem is solved naturally and *formally* – the incorrect semantic interpretations are excluded because they are ill-typed (in the empty context, where semantic interpretations of whole sentences like (8) are considered).

For example, (8) will be interpreted as (11), while the ‘incorrect’ interpretation (12) is not available (the formula (12) is ill-typed because  $x$  in  $Evt_A(x)$ , outside the scope of second/bound  $x$  (although intuitively it refers to it), is a free variable without being declared.)

- (11)  $\neg\exists x: \mathbf{e}. (dog(x) \ \& \ \exists e: Evt_A(x). bark(e))$   
 (12)  $(\#) \exists e: Evt_A(x). \neg\exists x: \mathbf{e}. dog(x) \ \& \ bark(e)$

This offers a natural solution to the event quantification problem. Compared with existing solutions with informal ad hoc principles such as those mentioned above, our solution comes naturally as a ‘side effect’ of introducing dependent event types: it is formally disciplined and natural.

### 5.2 EQP in MTT-semantic with Dependent Event Types

In this paper, we have focussed on extending the traditional Montague semantics with dependent event types (formally,  $C_e$ ), since the simple type theory is what the most semanticists are familiar with. One can also extend the MTT-semantic [4, 13] with dependent event types (formally,  $UTT[E]$ , if we use  $UTT$  for MTT-semantic) and hence consider such refined event semantics in the setting of MTT-semantic. Here, we give an example to show how this is done.

Still consider the sentence (8): No dog barks. In the MTT-semantic, where CNs are interpreted as types (rather than predicates), the verb **bark** is given a dependent type as its semantics:

- (13)  $bark: \Pi x: Dog. Evt_A(x) \rightarrow Prop$

It is also the case that the correct semantics (14) for (8) is legal (well-typed), while the incorrect one (15) is not:

- (14)  $\neg\exists x: Dog. \exists e: Evt_A(x). bark(x, e)$   
 (15) (#)  $\exists e: Evt_A(x). \neg\exists x: Dog. bark(x, e)$

Note that (15) is ill-typed for two reasons now: the first  $x$  is a variable not assumed anywhere and the term  $bark(x, e)$  is ill-typed as well.

Employing dependent event types in the Montagovian semantics (i.e., in  $C_e$  as described in Sect. 4.1), would still leave a small possibility of some formally legal but incorrect semantics. For instance, one might consider the following semantics for (8):

- (16) (#)  $\exists e: Event. \neg\exists x: \mathbf{e}. dog(x) \ \& \ bark(e)$

Note that, although (16) is incorrect, it is still well-typed because  $e$  is just an event, not an event with  $x$  as agent.<sup>9</sup> This, however, would not happen in the MTT-semantic setting where the type of the verb  $bark$  is the dependent type (13) and the following semantic sentence is ill-typed:

- (17) (#)  $\exists e: Event. \neg\exists x: Dog. bark(x, e)$ ,

because  $bark(x, e)$  is not well-typed (it requires  $e$  to be of type  $Evt_A(x)$ , not just of type  $Event$ ).

## 6 Conclusion

In this paper, we have introduced dependent event types for formal semantics. Subtyping is shown to play an essential role in this setting. We have also considered how dependent event types naturally solve the event quantification problem in combining event semantics with the traditional compositional semantics.

The notion of event types as studied in this paper is *intensional*, rather than extensional. For instance, when considering inverse verb pairs such as `buy` and `sell`, one may think that the events in (18) and (19) are the same [19].

- (18) John bought the book from Mary.  
 (19) Mary sold the book to John.

If one considers this from the angle of extensionality/intensionality, the buying event and the selling event in the above situation are extensionally the same, but intensionally different. More generally, this is related to how to understand the sameness of events in the setting with dependent event types. Work need be done to study event structures and relevant inference patterns.

Another interesting research topic is to study whether all thematic roles should be considered as parameters of dependent event types. Unlike agents and patients, some thematic roles considered in the literature may not be suitable to play the role of indexing dependent event types. In such cases, we would still propose that they should be formalised by means of logical predicates/relations. In the other direction, event types may depend on other entities other than thematic roles and further studies are called for to understand this better.

<sup>9</sup> Of course, one can argue that this is not intended since the agent is known, but formally, nothing prevents one from doing it.

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