

# Dependent Event Types

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Employing dependent types for a refined treatment of event types provides a nice improvement to Davidson’s event semantics [3, 7]. We consider dependent event types indexed by thematic roles and show that subtyping between them plays an essential role in semantic interpretations. It is also shown that dependent event types give a natural solution to the event quantification problem in combining event semantics with the Montague semantics [1, 8, 4].

For instance,  $Evt_A(a)$  is the dependent type of events whose agents are  $a : Agent$ . The dependent event types abide by subtyping relationships:

$$Evt_{AP}(a, p) \leq Evt_A(a) \leq Event \quad \text{and} \quad Evt_{AP}(a, p) \leq Evt_P(p) \leq Event,$$

where  $a : Agent$ ,  $p : Patient$  and  $Event$  is the type of all events. With such dependent event types, subtyping is crucial. Consider **John talked loudly**: its Davidsonian event semantics would be  $\exists e : Event. talk(e) \& loud(e) \& agent(e, j)$ , where  $talk, loud : Event \rightarrow \mathbf{t}$ . With dependent event types, the semantics would be  $\exists e : Evt_A(j). talk(e) \& loud(e)$ , in which the terms such as  $talk(e)$  are only well-typed because  $Evt_A(j) \leq Event$ .

It has been argued that there is some incompatibility between (neo-)Davidsonian event semantics and the traditional compositional semantics, as the event quantification problem shows: the following two possible interpretations of **No dog barks** are both well-formed formulas, although (2) is incorrect:

- (1)  $\neg \exists x : \mathbf{e}. dog(x) \& \exists e : Event. bark(e) \& agent(e, x)$
- (2)  $(\#) \exists e : Event. \neg \exists x : \mathbf{e}. dog(x) \& bark(e) \& agent(e, x)$

To exclude such incorrect interpretations, various informal solutions have been proposed [1, 8]. With dependent event types, this problem is solved naturally and formally – the incorrect semantic interpretations such as (4) below are excluded because they are ill-typed, while the correct one (3) is well-typed.

- (3)  $\neg \exists x : \mathbf{e}. (dog(x) \& \exists e : Evt_A(x). bark(e))$
- (4)  $(\#) \exists e : Evt_A(x). \neg \exists x : \mathbf{e}. dog(x) \& bark(e)$

The underlying formal system  $C_e$  is the extension of Church’s simple type theory [2], as used in the Montague semantics, with dependent event types and the subtyping relations.  $C_e$  can be faithfully embedded into  $UTT[C]$ , i.e., the type theory  $UTT$  [5] extended with coercive subtyping in  $C$  [6], where  $C$  contains the subtyping judgements that correspond to the above subtyping relations between

dependent event types. Since  $UTT[C]$  has nice meta-theoretic properties such as normalisation and logical consistency, so does  $C_e$ .

The paper is available online at <http://www.cs.rhul.ac.uk/home/zhaohui/DET.pdf>.

## References

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